Modified compact tension specimen for experiments on cement based materials: comparison of calibration curves from 2D and 3D numerical solutions

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ABSTRACT. The evaluation of fracture mechanics parameters of materials has become very important part of considering the condition of older constructions as well as properties of newly developed materials. This contribution focuses on a numerical simulation and a calculation of fracture mechanical properties of modified compact tension test configuration. It is possible to prepare the specimens used for this test very easily from a drilled core or from specimens used for cylindrical compression test. The focus of contribution is to compare selected outputs from numerical solution of 2D (plane strain conditions) with 3D models. Particularly, the determination of the influence of 2D and 3D model on the calibration curves for selected fracture mechanics parameters is of interest.Finite element software ANSYS was used for the numerical analysis.

KEYWORDS. Stress Intensity Factor; COD; CMOD; Biaxiality Factor; Modified Compact Tension Test; Fracture Mechanics of Concrete.

INTRODUCTION

Compact tension (CT) tests have been widely and successfully applied for measuring the fracture properties of several materials, such as metals (ASTM Standard E-399 [3]), or even composite materials with limited orthotropy [1]. Note that for test of fracture properties is not prepared norm only recommendation RILEM for three point bending test [17], RILEM for bending test for concrete with fibers [16, 18] and as a standard test the wedge splitting test is used (cube or cylindrical [12, 14, 19, 20]). The compact tension fracture toughness test (CT test [11, 22]) is essentially performed by applying equal and opposite forces through two holes previously made in the specimen, to propagate an initial crack. However, its applicability in concrete is characterized by some disadvantages, such as drilling the holes necessary to apply
the pulling forces and the hazard of a local fracture originated at these holes. The modified compact tension test (MCT [4, 5, 9, 10, 21, 23]) is a quite new test configuration on notched specimens to obtain fracture mechanics parameters of materials in laboratory conditions, note that test is derived from classic CT test. A detailed research program/campaign has to be done before the configuration starts to be used as a standard.

The several authors used cohesive crack model and prepared MCT model in software ATENA [10] or in software ABAQUS [5]. Pilot experimental measurement and comparison of selected configurations with three point bending specimen is introduced in contributions [4, 9].

The main advantage of MCT test is a round shape of the specimen that makes it appropriate for testing cement based composites. Due to its shape, it is easy to prepare specimen both ways: by cutting them of the drilled core in case of constructions which are already being used [6-8, 15] as well as in forms from the fresh concrete mixture [24]. The geometry of the specimen is shown in Fig. 1.

The aim of the paper is to provide calibration curves according to four different fracture mechanics parameters and to compare selected case with the values obtained from 3D model with the results from 2D model, which have already been published in [21]. The first considered parameter is stress intensity factor \( K_I \) [MPa\( \cdot \)m\(^{1/2} \)], see e.g. [1, 3, 11]. The value of stress intensity factor for each normalized crack length \( a/W \) is obtained by linear extrapolation from values in particular nodes behind the crack tip up to 3 mm distance. Values in a number of first nodes had to be neglected due to big mistake caused by stress singularity near to the crack tip. Values of T-stress [MPa] defined e.g. were obtained by different method.

Both parameters were normalized as dimensionless biaxiality factors \( B_1 [-] \) and \( B_2 [-] \) by (1) using the Eqs. (2) and (3), see [11, 13]:

\[
K_0 = \frac{P}{t \cdot W}, \tag{1}
\]

\[
B_1 = \frac{K_i}{K_0}, \tag{2}
\]

\[
B_2 = \frac{T \cdot \sqrt{\pi a}}{K_i}, \tag{3}
\]

where \( P \) is loading force in [N], \( t \) is thickness of the specimen in [mm], \( W \) stands for the position of loading force in [mm] and \( a \) is the crack length in [mm].

![Figure 1: Modified compact tension test: a) schema of the test and b) a photo from the test.](image)
The next two considered parameters were opening displacements. The first, crack opening displacement COD [mm] is an opening displacement under the load force (at loadline), 5 mm from the crack path. The second one, crack mouth opening displacement CMOD [mm] is measured at crack edge. In both cases, the outputs were dimensionless compliance functions $f_{COD}(a/W)$ [-] and $f_{CMOD}(a/W)$ [-] obtained from measured values of displacement by using normalization Eq. (4) in the Eq. (5).

$$f_{\text{norm}} = \frac{K}{2E\sqrt{\pi}} \frac{1}{a/W},$$  \hspace{1cm} (4)

$$f(a/W) = \frac{u_y}{f_{\text{norm}}},$$  \hspace{1cm} (5)

where $u_y$ is selected point displacement in [mm], $\nu$ is Poisson’s ratio [-] and $E$ is Young’s modulus [MPa]. The positions of selected points are related to the experimental set-up position: CMOD-clip gage at the end of specimen and COD – by displacement of machine load set up or both (CMOD, COD) points by system ARAMIS or other digital image correlation system. The considered values of material characteristics are summarized in Tab. 1.

<table>
<thead>
<tr>
<th>Elastic properties</th>
<th>$E$ [MPa]</th>
<th>$\nu$ [-]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Steel</td>
<td>210 000</td>
<td>0.3</td>
</tr>
<tr>
<td>Concrete - 5</td>
<td>5 000</td>
<td>0.2</td>
</tr>
<tr>
<td>Concrete - 20</td>
<td>20 000</td>
<td>0.3</td>
</tr>
<tr>
<td>Concrete - 25, see [21]</td>
<td>25 000</td>
<td>0.2</td>
</tr>
<tr>
<td>Concrete - 60</td>
<td>60 000</td>
<td>0.2</td>
</tr>
<tr>
<td>Concrete - 100</td>
<td>100 000</td>
<td>0.2</td>
</tr>
</tbody>
</table>

Table 1: Characteristics of used materials as the input parameters for numerical calculation.

**Numerical solution**

In this paper, the 2D and 3D models for numerical solution will be compared in a range of two-parameter fracture mechanics (see [11, 20]). The finite element software ANSYS was used for numerical analysis [2]. Element type PLANE183 was used for 2D simulation which is able to degenerate from 8-node to 6-node and therefore is able to fit better stress singularity due to translocate to middle node to $1/4$ distance from crack tip. For 2D model, the plane-strain conditions were applied due to experiment specimen thickness 50 mm. The 2D solution is described and discussed in [21]. For 3D model, the element SOLID186 was used. This type of element is suitable for irregular meshes, tetrahedral and pyramid options could be used. The specimen thickness for 3D model was 50 mm (full specimen).

A diameter of specimen used for simulations was selected as $D=150$ mm as an appropriate size of a drill which is commonly used to obtain this type of specimen from a construction element. A considered length of the steel bars was 110 mm on each side of the specimen and used load force was $P=1500$ N. The load force was applied as a pressure on the area at the end of the bar so the stress was applied uniformly. The end part of the steel bar (last 30 mm) was considered to be gripped into hydraulic testing machine. Therefore for this part, a displacement in $x$ and $z$ directions was set to zero. The diameter of the steel bars was 8 mm. An interface among the steel bar and a concrete matrix was modeled without any transitional layer (perfect adhesion). The perpendicular distance between steel bars and the middle of the specimen was 45 mm. A relative crack length $\alpha$ (stands for $a/W$ ratio) varied from 0.1 to 0.9 in steps of 0.1.

The density of the mesh was refined in the vicinity of the crack tip, where average element size was 0.2 mm. Then the element size fluently increases to the value of 5 mm on the outer sides of the specimen. The advantage of symmetric specimen was exploited and so only 1/4 of 3D model was built. The symmetric boundary conditions were applied along the vertical cross-section. The meshed model for $\alpha=0.4$ is shown in Fig. 2.
NUMERICAL RESULTS AND DISCUSSION

The finite element simulations were performed for various values of material properties listed in Tab. 1 (effect of change elasticity modulus ratio – constant value of Young’s modulus for steel and the value of Young modulus for concrete is changed), and effect of 2D and 3D model solutions for various crack lengths, subjected to uniform load. The results of stress intensity factors $K$ and $T$-stress are normalized by Eq. (2) and (3). In Figs. 3 and 8, the examples of deformed finite element models of 2D and 3D solutions are shown. The calibration curves are introduced in Eqs. (6-24) for each selected case.

Figure 2: Example of finite element 3D model used for numerical study $\alpha=0.4$.

Effect of elasticity modulus ratio
The numerically obtain results from 2D model solution covering the effect of elastic modulus ratio are shown in Figs. 4-7 (stress intensity factor, $T$-stress, COD and CMOD). The results of stress intensity factors and $T$-stress are normalized by Eqs. (2) and (3).
The functions of the calibration curve for MCT specimens with steel bars with diameter 150 mm have to be calculated for each value of Young’s modulus, especially, for long cracks from 0.6 to 1, see example for selected values.

Figure 3: Example of 2D finite element model after deformation.
The $B_1$ curves are practically the same values for all five various materials. It only changes for values of relative crack length longer than $\alpha = 0.5$ (see Fig. 4). The functions of calibration curves for selected Young's modulus of concrete $E= 5, 20$ and 100 GPa can be introduced as follows:

\[
B_1 (E=5) = 5.5881 - 34.181\alpha + 239.39\alpha^2 - 594.79\alpha^3 + 688.58\alpha^4 - 251.61\alpha^5 \quad (6)
\]

\[
B_1 (E=20) = -2.3617 + 117.22\alpha - 736.11\alpha^2 + 2191.5\alpha^3 - 2926.8\alpha^4 + 1503.9\alpha^5 \quad (7)
\]

\[
B_1 (E=100) = -16.91 + 389.22\alpha - 2465.6\alpha^2 + 7030.8\alpha^3 - 9049.3\alpha^4 + 4371.4\alpha^5 \quad (8)
\]

Figure 4: Values of dimensionless $B_1$ factor (stress intensity factor) versus $a/W$, the effect of elasticity modulus ratio (steel $E=210$ GPa).

Fig. 5 shows that the $B_2$ parameter changes practically negligibly, only for very low values of Young's modulus $E=5$ GPa, there is relatively small deviation from another curves.

Figure 5: Values of dimensionless $B_2$ factor ($T$-stress) versus $a/W$, the effect of elasticity modulus ratio (steel $E=210$ GPa).
Compliance functions (according Eqs. (4) and (5)) for opening displacement under the loading force (COD) and for opening displacement at the crack mouth (CMOD) follow for Young's modulus of concrete $E=5$, 20 and 100 GPa, respectively:

for COD

$$B_2 (E=5) = -0.5625 + 5.0149\alpha - 7.4585\alpha^2 + 5.1659\alpha^3 - 0.636\alpha^4$$  \hspace{1cm} (9)

$$B_2 (E=20) = -0.4339 + 3.7445\alpha - 2.3166\alpha^2 + 2.6828\alpha^3 - 3.5752\alpha^4$$  \hspace{1cm} (10)

$$B_2 (E=100) = -0.2136 + 1.0257\alpha + 7.8949\alpha^2 - 17.492\alpha^3 + 10.933\alpha^4$$  \hspace{1cm} (11)
\begin{equation}
\begin{aligned}
    f_{\text{COD}} (E=5) &= 6.0419 - 4.4767\alpha + 77.12\alpha^2 - 153.38\alpha^3 + 106.59\alpha^4 \\
    f_{\text{COD}} (E=20) &= 6.7211 - 12.764\alpha + 111.24\alpha^2 - 208.43\alpha^3 + 138.35\alpha^4 \\
    f_{\text{COD}} (E=100) &= 7.491 + 21.077\alpha + 139.81\alpha^2 - 248.63\alpha^3 + 158.95\alpha^4
\end{aligned}
\end{equation}

and for CMOD

\begin{equation}
\begin{aligned}
    f_{\text{CMOD}} (E=5) &= 10.54 - 10.549\alpha + 100.94\alpha^2 - 194.05\alpha^3 + 132.77\alpha^4 \\
    f_{\text{CMOD}} (E=20) &= 12.478 - 27.907\alpha + 162.68\alpha^2 - 285.45\alpha^3 + 182.31\alpha^4 \\
    f_{\text{CMOD}} (E=100) &= 15.905 - 55.717\alpha + 245.61\alpha^2 - 390.95\alpha^3 + 231.39\alpha^4
\end{aligned}
\end{equation}

Effect of 2D and 3D model solutions

The results of 2D and 3D model solutions (steel \( E = 210 \) GPa, concrete \( E = 25 \) GPa) are shown in Figs. 9-12 (stress intensity factor, \( T \)-stress, COD and CMOD). The model of 3D model solution was prepared as \( 1/4 \) of all body, the steel part was as \( 1/2 \) of the round bar. The example of the model after deformation is shown in Fig. 8.

![Figure 8: Example of 3D finite element model after deformation.](image)

![Figure 9: Values of dimensionless \( B_1 \) factor (stress intensity factor) versus \( a/W \), effect of elasticity modulus ratio (steel \( E = 210 \) GPa).](image)
The $B_1$ curves are practically the same for both cases. It only changes for values of relative crack length longer than $\alpha = 0.7$ (see in Fig. 9). The functions of calibration curve for both (2D and 3D) solutions (with Young’s modulus of concrete $E = 25$ GPa) can be introduced as follows:

$$B_1 (2D) = -4.4888 + 157.35\alpha - 992.61\alpha^2 + 2913.2\alpha^3 - 3845.6\alpha^4 + 1937.8\alpha^5$$  \hspace{1cm} (17)

$$B_1 (3D) = -19.17 + 437.74\alpha - 2795.2\alpha^2 + 7977.5\alpha^3 - 10259\alpha^4 + 4936.2\alpha^5$$  \hspace{1cm} (18)

Fig. 10 shows that the $B_2$ parameter changes practically negligibly. Only for very long cracks 0.7 and longer, some differences can be seen between curves.

$$B_2 (2D) = -0.352 + 2.6238\alpha + 2.2014\alpha^2 - 9.8235\alpha^3 + 7.4131\alpha^4$$  \hspace{1cm} (19)

$$B_2 (3D) = -0.2905 + 2.2439\alpha + 2.305\alpha^2 - 8.4968\alpha^3 + 6.315\alpha^4$$  \hspace{1cm} (20)

The curves obtained by 3D model solution do not differ very much and they follow the shape of ones obtained by 2D model solution. The main differences come for relative long crack $\alpha = 0.8$ for the values of stress intensity factor results, see...
The obtained values are a little higher over a whole range of relative crack length and that’s caused by $\gamma$ stress component.

Compliance functions for opening displacement under the loading force (COD) and for opening displacement at the crack mouth (CMOD) (according Eqs. (4) and (5)) follow from 2D and 3D model solutions, respectively:

for COD

$$f_{\text{COD}}(2D) = 6.8209 - 13.922\alpha + 115.54\alpha^2 - 214.86\alpha^3 + 141.81\alpha^4$$  \hspace{1cm} (21)

$$f_{\text{COD}}(3D) = 7.7038 - 18.056\alpha + 131.72\alpha^2 - 239.55\alpha^3 + 155.85\alpha^4$$  \hspace{1cm} (22)

and for CMOD

$$f_{\text{CMOD}}(2D) = 12.849 - 31.071\alpha + 172.7\alpha^2 - 298.93\alpha^3 + 188.98\alpha^4$$  \hspace{1cm} (23)

$$f_{\text{CMOD}}(3D) = 15.138 - 43.207\alpha + 210.8\alpha^2 - 350.23\alpha^3 + 215.04\alpha^4$$  \hspace{1cm} (24)

Figure 12: Values of CMOD (crack mouth open displacement) versus $a/W$, the effect of elasticity modulus ratio (steel $E=$210 GPa).

**CONCLUSIONS**

The finite element analysis of two effects on modified compact tension test for specimens like concrete is introduced by means of a constraint-based two parameter fracture mechanic approach. Five various materials configurations (steel and concrete) and 2D and 3D solutions were investigated. The following principal conclusions could be derived:

- The influence of elasticity modulus ratio (constant value of Young’s modulus defined for steel and different values for concrete) on the calibration curve is not negligible and for each case a different polynomial function has to be used.
- The curves obtained by 3D model solution don’t differ very much and they follow the shape of ones obtained with 2D model solution very well, the largest differences are related to long crack in stress intensity factor results. The obtained values are a little higher over a whole range of relative crack length and that’s caused by $\gamma$ stress component.
- The results from 2D model solution can be used instead of ones from 3D model solution and they are in a range of acceptance. Moreover, they can be calculated much faster for another specimen sizes or bars positions.
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