Creep-fatigue life evaluation of high chromium ferritic steel under non-proportional loading

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ABSTRACT. T Multiaxial creep-fatigue tests under non-proportional loading conditions with various strain rates were carried out using a hollow cylinder specimen of a high chromium ferritic steel at 823K in air to discuss the influence of non-proportional loading on failure life. Strain paths employed were a push-pull loading and a circle loading. The push-pull loading test is proportional strain path test. The circle loading test is non-proportional strain path test in which sinusoidal waveforms of axial and shear strains have 90 degree phase difference. The failure life is affected largely by the strain rate and the non-proportional loading. This paper presents a modified strain range for life evaluation considering the strain rate based on a non-proportional strain parameter proposed by authors. The strain range is a suitable parameter for life evaluation of tested material under non-proportional loading at high temperature.

KEYWORDS. Life evaluation; Creep-fatigue; Multiaxial strain; Non-proportional loading; High chromium ferritic steel.

INTRODUCTION

In the blanket structure of a demonstration fusion reactor, the material receives severe cyclic loading conditions such as combined thermal and mechanical cyclic deformations. By the combination of thermal and mechanical loading, the non-proportional loading in which the principal stress and strain directions rotate in a cycle occurs. It has been
reported that failure lives are reduced accompanying with an additional hardening due to non-proportional loading depending on both the strain path and the material [1-5]. The failure life under non-proportional loading at high temperature has been discussed in the previous study for the high chromium ferritic steel [6]. However, open questions of discussing creep-fatigue property still exist. Therefore, creep-fatigue test results and damage evaluation under multiaxial loading are required for reliable and safety design of strength for materials and components. 

In this study, creep-fatigue tests under a push-pull loading and a circle loading conditions with changing the strain rate were performed at 823K in air. The evaluation of failure life is also discussed from the obtained test results.

**EXPERIMENTAL PROCEDURE**

Multiaxial creep-fatigue tests under non-proportional loading with various waveforms were carried out at 823K in air. A hollow cylinder specimen which has a 9mm inner-diameter, a 12mm outer-diameter and a 12mm in a gauge length as shown in Fig. 1 was employed. The testing machine used was an electrical servo hydraulic tension and torsion fatigue testing machine. Strain paths and strain waveforms are shown in Fig. 2. They are the push-pull loading (PP) and the circle loading (CI). The PP test is the proportional strain loading test. The CI test is the non-proportional strain loading test in which axial strain and shear strain have 90 degree sinusoidal out-of-phase. Total axial strain and total shear strain ranges were the same ranges based on von Mises basis ($\Delta \varepsilon = \Delta \gamma / \sqrt{3}$). In these strain paths, three strain rates were employed. They are 0.2%/s, 0.01%/s and 0.002%/s based on von Mises basis which are indicated by ‘FF’, ‘SS’ and ‘SS*’, respectively. Strain holdings are also employed, they are the tensile and the compressive holdings which are indicated by ‘TH’ and ‘CH’. The holding times used were 180s (3min.) and 600s (10min.).

Number of cycles to failure (failure life) $N_f$ is defined as the cycles at which the axial or shear stress was reduced to 3/4 of the sudden decrease point.
EXPERIMENTAL RESULTS AND DISCUSSION

Failure Life

Tab. 1 and Fig. 3 show the test results and the failure life. The failure life is affected largely by not only strain path (strain non-proportionality) but also strain waveform (creep damage). In the PP test, the failure life is reduced with the decrease in the strain rate under the same strain range, which may be resulting from larger creep damage caused by the lower strain rate. On the other hand, in the CI test, the failure life is increased when the strain rate is reduced from 0.2%/s to 0.01%/s, but the failure life is decreased by the further reduction in the strain rate from 0.01%/s to 0.002%/s. The former may be resulting from the reduction in the intensity of strain non-proportionality caused by stress relaxation due to creep and the latter can by the increase of creep damage.

<table>
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<tr>
<th>Strain path</th>
<th>Waveform</th>
<th>Strain rate (%/s)</th>
<th>Holding time (s)</th>
<th>Δεeq (%)</th>
<th>Nf (cycles)</th>
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Table 1: Test conditions and results.

Fig. 4 shows a correlation of the failure life by von Mises’ equivalent strain range Δεeq. In the figure, a bold solid line is drawn based on the data in the PP-FF test which is the life curve for life evaluation and two thin lines show a factor of 2 band. The bold solid line is given by

\[
\Delta \varepsilon_{\text{eq}} = AN_f^{-0.12} + BN_f^{-0.6}
\]

(1)

where the coefficients A and B are defined as 3.5σ_y/E and ε_0.6 according to the definition of the universal slope method [7]. In this study, B is put as the curve to be fit with the data in the PP-FF test. This figure shows clearly a large reduction in the failure life in the CI test compared with the PP test according to the non-proportional loading effect.
failure life $N_f$, cycles

Strain range $\Delta \varepsilon_{eq}$

**Figure 3:** Comparison of creep-fatigue failure lives.

In multiaxial low cycle fatigue tests, it has been reported that the large reduction in the failure life has a close relation with strain path and material. Itoh et al. [8-13] proposed a non-proportional strain range $\Delta \varepsilon_{NP}$ for life evaluation under non-proportional loading defined by

$$\Delta \varepsilon_{NP} = (1 + \alpha f_{NP}) \Delta \varepsilon_1$$

where $\Delta \varepsilon_1$ is a maximum principal strain range under non-proportional loading which can be calculated by $\varepsilon$ and $\gamma$. $\alpha$ and $f_{NP}$ are a material constant and a non-proportional factor, respectively. The former is the parameter related to the additional hardening due to non-proportional loading and the latter is the parameter expressing the intensity of non-proportional loading. The value of $\alpha$ is the ratio to fit the failure life in the CI test to that in the PP test at the same $\Delta \varepsilon_1$. $f_{NP}$ is defined by [12]
\[ f_{NP} = \frac{\pi}{2 S_{max}} \int_{c} |\mathbf{e}_i \times \mathbf{e}_R| S_i(t) \, ds, \quad L_{path} = \int_{c} ds \]  

(3)

where \( S_i(t) \) is the maximum absolute value of principal strains at time \( t \), \( S_{max} \) is the maximum value of \( S_i(t) \). \( \mathbf{e}_i \) and \( \mathbf{e}_R \) are unit vectors of \( S_{max} \) and \( S_i(t) \), \( ds \) the infinitesimal trajectory of the loading path. \( L_{path} \) is the whole loading path length during a cycle and “\( \times \)” denotes vector product. Integrating the product of amplitude and principal direction change of stress and strain by path length in Eq. (3) is a suitable parameter for evaluation of the additional damage due to non-proportional loading. Detail descriptions of \( f_{NP} \) and the life evaluations have been mentioned in reference [12] and are omitted here. \( f_{NP} \) in the PP test (proportional loading) takes 0 and that in the CI (non-proportional loading) takes 1.

Fig. 5 shows a correlation of the failure life by \( \Delta \varepsilon_{NP} \). This figure shows that dark symbols for PP-FF and CI-FF tests are plotted beside the bold line and \( \Delta \varepsilon_{NP} \) can evaluate non-proportional loading tests at the high strain rate. Because of creep damage, the failure lives in lower strain rates are scattered even though almost all data are correlated within the factor of 2 band. Therefore, \( \Delta \varepsilon_{NP} \) may need some modification which considers the effect of strain rate.

Creep Fatigue Damage under Proportional Loading Condition

The evaluation method proposed by Coffin [14], which takes into account the strain rate under proportional loading, is employed for life evaluation. The equation is given by

\[ \Delta \varepsilon_p (v^{k-1} N_f)^\beta = C \]  

(4)

where \( \Delta \varepsilon_p \) and \( v \) are plastic strain and cyclic frequency. \( C, \beta \) and \( k \) are material constants. From the experimental results in PP-FF and PP-SS tests, the material constants and a correlation of strain ranges in PP-FF and PP-SS tests can be calculated by Eq. (5).

\[ \Delta \varepsilon_{PP-FF} = \Delta \varepsilon_{PP-SS} \left( \frac{v}{v_0} \right)^{(k-1)\beta} \]  

(5)
In this material at the tested temperature, $k$ and $\beta$ take 0.6 and 0.9, respectively. $\Delta e^{\text{PP-FF}}_P$ and $\Delta e^{\text{PP-SS}}_P$ are plastic strain ranges when $N_i$ in PP-FF test takes the same value as that of PP-SS test. According to that correlation in this figure, a modified strain range $\Delta e^{\text{NP}}_P$ can be defined as,

$$\Delta e^{\text{NP}}_P = (1 + a f_{\text{NP}})K_v \Delta e_1 \quad K_v = \left(\frac{v}{v_0}\right)^{(k-1)\beta}$$  \hspace{5cm} (6)

where $v_0$ is the frequency at the strain rate of the fatigue test in which creep effect can be ignored. In this study, the strain rate in the PP-FF test is set as $v_0$. $v$ is an arbitrary frequency in the tests with the lower strain rate of which creep effect is included. PP-TH, PP-CH and CI-TH tests which have strain holding are assumed to be transformed proximately into the test of triangular or sinusoidal waveform with low strain rate. Fig. 6 shows how to transform the strain waveform in the holding test into an equivalent strain waveform to obtain the strain rate $v'$. The strain rate is calculated from the equivalent strain waveform. Fig. 7 shows a correlation of the failure life by $\Delta e^{\text{NP}}_P$. The data in PP test under various strain rates including strain holding is correlated within the factor of 2 band even though data in high strain ranged tests are plotted conservatively. On the other hand, the data in CI test under low strain rates is underestimated.

**Figure 6: Assuming waveform of hold loading equivalent to triangular loading.**

**Creep Fatigue Damage under Non-proportional Loading Condition**

The low strain rate reduces the failure life by creep damage. On the other hand, the intensity of strain non-proportionality decreases due to the stress relaxation caused by creep. For the life evaluation in low strain rates under non-proportional loading, a modified non-proportional strain range is proposed by Eq. (6) by adding a new parameter $K_s$, which shows the reduction of intensity of non-proportionality. The modified strain range is given by

$$\Delta e^{\text{NP}}_P = (1 + a K_s f_{\text{NP}})K_v \Delta e_1 \quad K_s = \left(\frac{v}{v_0}\right)^{(k-1)\beta}$$  \hspace{5cm} (7)

where the value of $K_s$ is calculated from test results in CI test, that is, a correlation of $K_s$ with strain rate is obtained by data fitting. $\chi$ is a material constant, in case of this material $\chi=2.7$. 

![Diagram](image-url)
Fig. 8 shows a correlation of failure life by the modified non-proportional strain range. In the figure, all of the data can be plotted within the factor of 2 band. It suggests that $\Delta \varepsilon^*_{NP}$ becomes a suitable parameter for evaluation of the creep-fatigue failure life under non-proportional loading. Further creep-fatigue tests using other materials will be obtained for the discussion of this modified non-proportional strain range considering the strain rate.

**CONCLUSIONS**

(1) In the push-pull loading test (proportional loading test), failure life is decreased with decreasing in the strain rate resulting in creep damage.
(2) In the circle loading test (non-proportional loading test), failure life depends on the strain rate. The increase in the failure life can be explained by the reduction in the intensity of strain non-proportionality caused by stress relaxation due to creep. Conversely, the decrease in the failure life can be explained by the increase of creep damage.

(3) The modified non-proportional strain range considering the strain rate can correlate the failure life very well.

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